

Exercise 1

Plotting data

(handed out: 09.04.2025 – hand in: 16.04.2025)

Please, send in your solutions as a gzipped tarball or zip file with a distinct name, e.g., `dekon_elig_ex01.tgz`. This tarball should only contain printerfriendly PDFs, source code (e.g., `helloworld.cpp`), makefiles. Always provide source code as it is, i.e., not as text in a PDF file.

1. Task Plotting a histogram (3 P)

In the file `histo_data.txt` (click on [URL](#) or [embedded file](#)) you can find data from a simulation (one “measurement” x per line). Create a *normalized* histogram (i.e. with frequency of occurrence on the y-axis) of these data with a bin size of 0.1 together with the corresponding probability density function $\exp(-x)$. The output should be a PDF file.

2. Task Data plotting and transformation (9 P)

In an experiment of three series of measurements, the decay of ^{220}Rn (Thoron) was recorded with help of a Geiger-Müller counter. Determine the half-live $t_{1/2}$ of ^{220}Rn from the data (click on [URL](#) or [embedded file](#)):

- a) Derive and solve the differential equation for the radioactive decay, so that you get

$$N(t) = N_0 e^{-\lambda t}. \quad (1)$$

Start from the idea that the number of decayed nuclei $-dN$ within a time interval dt is proportional to the number of existing nuclei $N(t)$ with proportionality factor λ . (2P)

Also derive the relation between λ and $t_{1/2}$. (1P)

Of course, we cannot simply measure the amount of ^{220}Rn nuclei, but instead we measure the activity (count rate), why does this yield $t_{1/2}$? (1P)

- b) Use gnuplot or a similar plotting tool with PDF output, to plot the natural logarithm of the count rate (average of the three series) over time. Also plot a linear fit to these transformed data, yielding the half-life $t_{1/2}$. Use for the fit only the relevant data points, where the actual decay is measured, so for time interval [100 : 300]s. Do not forget to label axes, data, and curve. Hand in the PDF file. (4P)
Compare your result for $t_{1/2}$ with literature values (e.g., Wikipedia). (1P)